

## Derivative Rules



Name: \_\_\_\_\_

Date: \_\_\_\_\_

1. If  $f(x) = \sqrt{x-5}$ , then which one of the following is equal to  $f'(x)$ ?

A.  $\lim_{h \rightarrow 0} \frac{\sqrt{x+h-5} - \sqrt{x-5}}{5}$

B.  $\lim_{h \rightarrow 0} \frac{\sqrt{x+h-5} - \sqrt{x-5}}{h}$

C.  $\lim_{x \rightarrow 5} \frac{\sqrt{x-5} - \sqrt{h-5}}{h}$

D.  $\lim_{x \rightarrow 5} \frac{\sqrt{x+h-5} - \sqrt{h}}{h}$

2. If  $f(x) = 5x^3$ , then  $f'(2) =$

A. 30      B. 10      C. 60      D.  $15x^2$

3. If  $f(x) = \tan x$ , then  $f'(\frac{\pi}{3}) =$

A.  $\frac{1}{4}$       B.  $-\frac{1}{\sqrt{3}}$       C.  $\frac{\sqrt{3}}{2}$       D. 4

4. If  $f(x) = \sin x \cos x$ , then  $f'(\frac{\pi}{6}) =$

A.  $\sqrt{3}$       B.  $\frac{\pi^2}{3} - 1$   
C.  $\frac{1}{2}$       D.  $\frac{\pi^2}{3}$

5. Given  $f(x) = \frac{x}{\tan x}$ , find  $f'\left(\frac{3\pi}{4}\right)$ .

A.  $\frac{3\pi}{4} - 1$       B.  $\frac{-3\pi}{2} - 1$   
C.  $\frac{-3\pi}{4} - 1$       D.  $\frac{-3\pi}{4} + 1$

6. Differentiate:  $\frac{1 + \cos x}{1 - \cos x}$

A. -1      B.  $-2 \csc x$   
C.  $\frac{-2 \sin x}{(1 - \cos x)^2}$       D.  $\frac{-\sin^2 x}{(1 + \cos x)^2}$

7. Find the derivative,  $\frac{dy}{dx}$ , of  $y = \frac{2x}{1 - 3x^2}$ .

A.  $-\frac{1}{3x}$

B.  $-\frac{12x}{(1 - 3x^2)^2}$

C.  $\frac{6x^2 + 2}{(1 - 3x^2)^2}$

D.  $\frac{2x}{3(1 - 3x^2)^2}$

8. Assume  $f(7) = 0$ ,  $f'(7) = 14$ ,  $g(7) = 1$ , and  $g'(7) = \frac{1}{7}$ . Find  $h'(7)$  given  $h(x) = \frac{f(x)}{g(x)}$ .

A. -2      B. 14      C.  $\frac{49}{2}$       D. 98

9. The functions  $f$  and  $g$  are differentiable and have the values shown in the table.

If  $A = \begin{pmatrix} f & g \end{pmatrix}$ , then  $A'(4) =$

A. 0

B.  $-\frac{4}{9}$

C.  $\frac{1}{4}$

D.  $-\frac{1}{4}$

| x | f  | f' | g  | g'            |
|---|----|----|----|---------------|
| 0 | 5  | 1  | -7 | $\frac{1}{4}$ |
| 2 | 8  | 3  | -5 | 1             |
| 4 | 14 | 9  | -3 | 4             |
| 6 | 26 | 27 | -1 | 16            |

10. Find the derivative of  $y = (x^2 + 2x + 5)^6$ .

A.  $6(2x+2)(x^2 + 2x + 5)^5$

B.  $(12x+1)(x^2 + 2x + 5)^5$

C.  $\frac{2x+2}{(x^2 + 2x + 5)^6}$

D.  $\frac{6(2x+2)}{x^2 + 2x + 5}$

11. The functions  $f$  and  $g$  are differentiable and have the values shown in the table.

If  $A = \begin{pmatrix} f \\ g \end{pmatrix}$ , then  $A'(4) =$

- A. 0  
B.  $\frac{29}{9}$   
C.  $\frac{9}{4}$   
D.  $-\frac{83}{9}$

| $x$ | $f$ | $f'$ | $g$ | $g'$          |
|-----|-----|------|-----|---------------|
| 0   | 5   | 1    | -7  | $\frac{1}{4}$ |
| 2   | 8   | 3    | -5  | 1             |
| 4   | 14  | 9    | -3  | 4             |
| 6   | 26  | 27   | -1  | 16            |

12. Find the derivative:  $s(t) = \cos(\frac{t}{3})$

- A.  $3 \sin(\frac{t}{3})$   
B.  $\frac{1}{3} \csc(\frac{t}{3}) \cot(\frac{t}{3})$   
C.  $\frac{1}{3} \sin(\frac{t}{3})$   
D.  $-\frac{1}{3} \sin(\frac{t}{3})$

13. The functions  $f$  and  $g$  are differentiable and have the values shown in the table.

If  $A = f(g(x))$ , then  $A'(-8) =$

- A. -72  
B. 54  
C. 9  
D. -9

| $x$ | $f$ | $f'$ | $g$ | $g'$ |
|-----|-----|------|-----|------|
| -8  | 4   | 3    | -2  | 6    |
| -6  | 10  | 12   | 0   | 9    |
| -2  | 20  | 9    | 6   | 18   |
| 2   | 30  | 15   | 12  | 24   |

14. Find the derivative of  $y = \sqrt[3]{x^2 + x}$ .

- A.  $\frac{1}{3}(x^2 + x)^{-2/3}(2x + 1)$   
B.  $\frac{2}{3}(x^2 + x)^{-2/3}(2x - 1)$   
C.  $\frac{x}{3}(x + 1)^{-2/3}(2x + 1)$   
D.  $\frac{1}{3}(x^2 + x)^{2/3}(2x + 1)$

15. Find  $\frac{dy}{dx}$  for  $y = x^3 \sqrt{2x + 1}$

- A.  $\frac{x^2(7x + 3)}{\sqrt{2x + 1}}$   
B.  $\frac{3x^2}{2\sqrt{2x + 1}}$   
C.  $\frac{8x^3 + 3x^2}{2\sqrt{2x^4 + x^3}}$   
D.  $\frac{6x^3 + 3}{\sqrt{2x + 1}}$

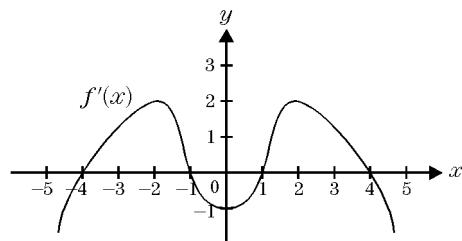
16.  $\frac{d}{da} \left( \frac{5}{(a^2 - 2)^4} \right) =$

- A.  $\frac{-40a}{(a^2 - 2)^3}$   
B.  $\frac{-40a}{(a^2 - 2)^5}$   
C.  $\frac{-20}{(a^2 - 2)^5}$   
D.  $\frac{20a^2}{(a^2 - 2)^3}$

17. If  $y = \frac{(4x - 3)^2}{\sqrt{x}}$ , then  $\frac{dy}{dx} =$

- A.  $\frac{3(4x - 3)}{2\sqrt{x^3}}$   
B.  $\frac{9(4x - 3)}{2x^{1/2}}$   
C.  $\frac{3(4x - 3)(4x + 1)}{2x^{3/2}}$   
D.  $3(4x - 3)x^{-3/2}$

18. The graph  $f(x)$  has horizontal tangents when  $x =$



- A. -2, 0, 2  
B. -2, 2  
C. -1, 2  
D. -4, -1, 1, 4

19. Find the derivative of  $y = \cos x^3$ .

- A.  $3x^2 \sin x^3$   
B.  $3 \cos x^3$   
C.  $-3x^2 \sin x^3$   
D.  $3x \cos x^2$

20. Find  $\frac{dy}{dx}$  if  $y = \sin^2 x - \cos^2 x$ .

- A.  $2 \sin 2x$   
B.  $2(\sin x - \cos x)$   
C.  $-2 \cos 2x$   
D.  $\cos^2 x - \sin^2 x$

21. If  $y = \sin(\cos x)$ , then  $\frac{dy}{dx} =$
- A.  $\sin x \cos(\sin x)$       B.  $-\sin x \cos(\cos x)$   
 C.  $3x^2 \sin x^3$       D.  $6x^2 \sin x^3 \cos x$
22. Find an equation for the tangent line to the graph of  $f(x) = \sqrt{x - 7}$  at the point where  $x = 16$ .
- A.  $x - 6y = -2$       B.  $6x - y = 2$   
 C.  $x - 6y = 2$       D.  $6x + y = -2$
23. The point  $\left(1, \frac{4}{3}\right)$  lies on the graph of  $f(x) = \frac{x+3}{x+2}$ . Find the slope of a line tangent to the graph at that point.
- A.  $-\frac{5}{9}$       B.  $-\frac{1}{9}$       C.  $\frac{1}{9}$       D.  $\frac{3}{2}$
24. The graph of  $f(x) = \frac{3x^2}{16-x^2}$  has a horizontal tangent at  $y =$
- A.  $-3$       B.  $3$       C.  $4$       D.  $0$
25. Given a function defined by  $f(x) = (x)^{1/3}(4 - x)$ , for what value(s) of  $x$  does the function have one or more vertical tangents?
- A.  $-2$  only      B.  $0$  only  
 C.  $4$  only      D.  $2, -4$